

# MITL Specification Debugging for Monitoring of Cyber-Physical Systems

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**1st Workshop on Monitoring and Testing of Cyber-Physical Systems**

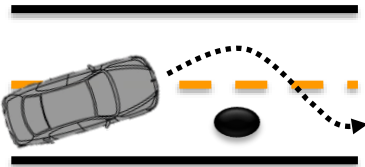
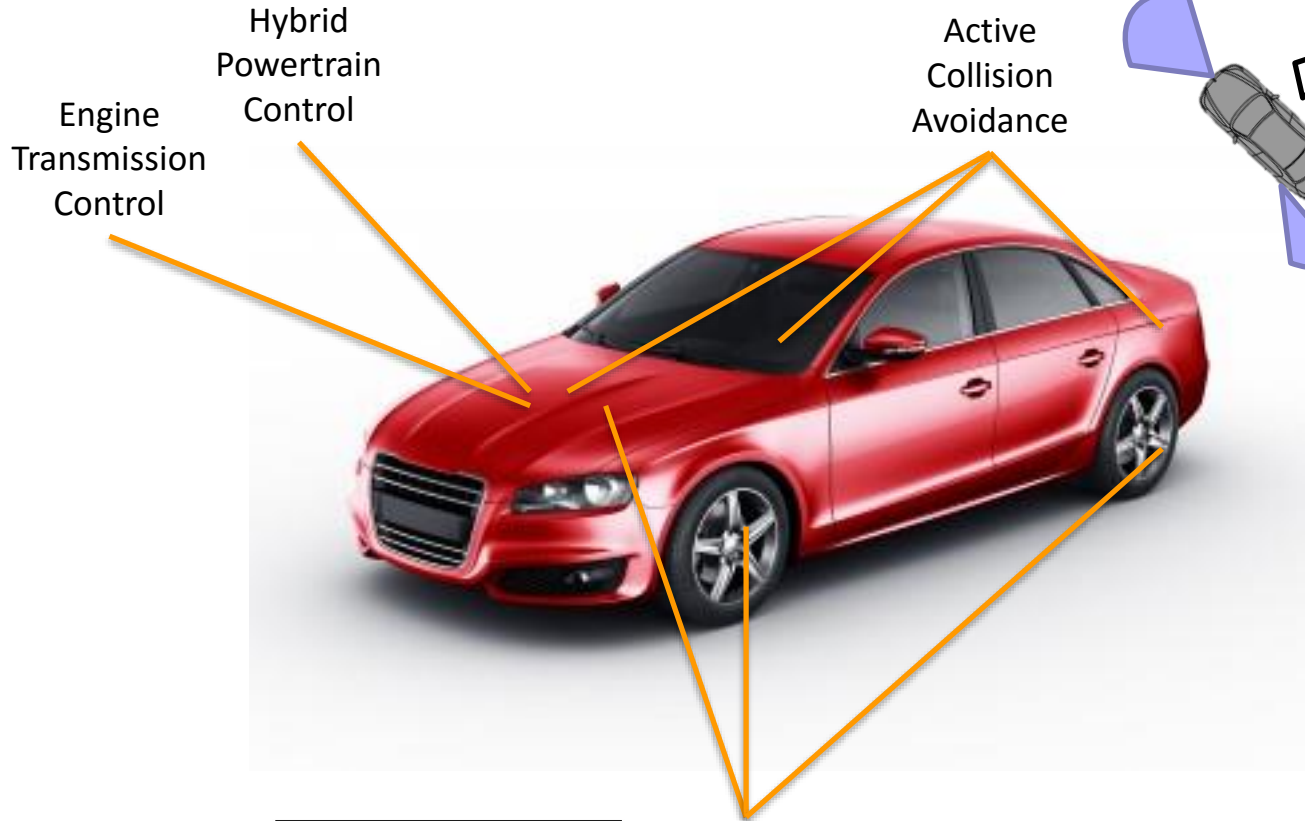
**April 2016**

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# Modern Vehicles



Electronic Stability Control

### Already demonstrated:

- Lane following
- Fully autonomous driving

# Trust? : Sampling of automotive recalls (~2011-12) due to software errors ...

- "A software error ... shifting from 5th to 4th gear when ... this may result in decreased engine ..."

No downshifting from 5<sup>th</sup> to 4<sup>th</sup>
- ... the software that "allows the ECU to establish a 'handshake' with the engine is in error. The ECU monitors ... of tolerance, the software pic ... code. As the ECU tries to find an ... rough idle or stalling situation ensues."

Rough idling or stalling due to complicated adaptive ECU
- ... to up ... instances, it is possible ... on opposite ...

Electric motor to rotate in the direction opposite to that selected by the transmission
- If the fault occur ... while driving - which would me ... steering. Braking or pressing the ...

Cruise control does not disengage unless turning off the ignition
- ...

Many more ...

# Trust? : Sampling of automotive recalls (~2011-12) due to software errors ...

- "A software error caused the vehicle to shift from 5th to 4th gear when the driver was in 5th gear. This may result in decreased engine performance."

Under C(x,p) conditions the system should always switch from 5<sup>th</sup> to 4<sup>th</sup> gear.
- ... the software that "allows the ECU to establish a 'handshake' with the engine is in error. The ECU monitors engine speed. If the engine speed is out of tolerance, the software prevents the engine from starting. As the ECU tries to find an appropriate engine speed through idle or stalling situation ensues."

The engine should never stall while idle.
- ... to upshift. In some circumstances, it is possible for the engine to rotate in the opposite direction of the transmission."
 

The electric motor should always rotate in the direction selected by the transmission.
- If the fault occurred while driving - which would cause the vehicle to lose steering. Braking or pressing the brake pedal would cause the vehicle to stop.

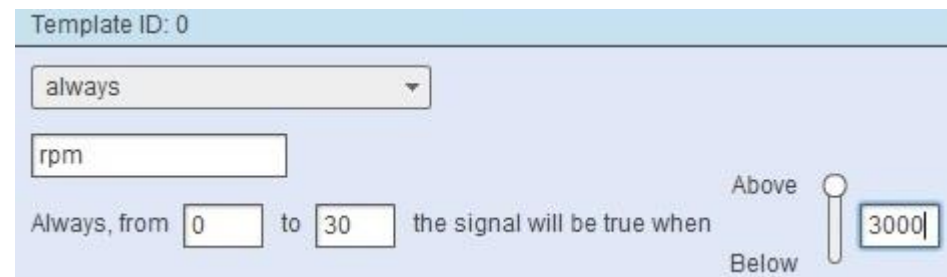
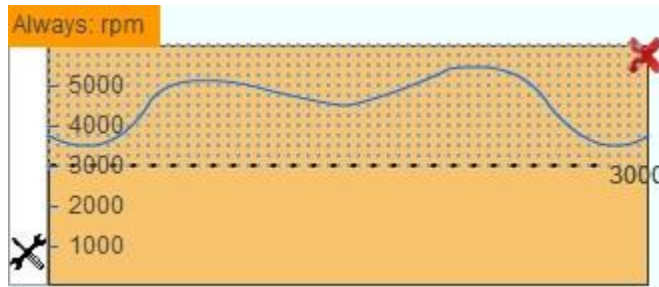
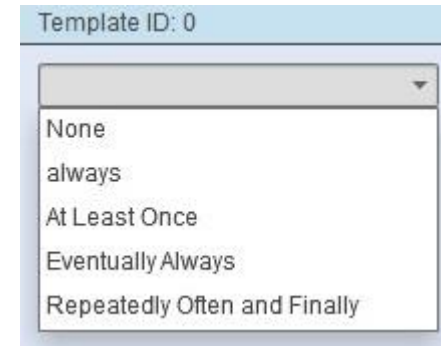
The cruise control should always disengage when the "turn off" button is pressed.
- ...

# Formal Specification

- Natural Language is not appropriate for verification
  - Ambiguous, inaccurate, inconsistent?
- Alternative: use mathematical logic
  - Elicitation process: Challenging & Error prone
- Validate the specification
  - Verification with wrong specification is useless
- Before verification we need to analyze the specification

# Previous Work: ViSpec

- ViSpec helps transforming Pre-specified templates in NL
- Easy to use
- No need for MITL background



- B. Hoxha and H. Bach and H. Abbas and A. Dokhanchi and Y. Kobayashi and G. Fainekos, **Towards Formal Specification Visualization for Testing and Monitoring of Cyber-Physical Systems**, DIFTS 2014
- B. Hoxha and N. Mavridis and Georgios Fainekos, **VISPEC: A graphical tool for easy elicitation of MTL requirements**, IROS 2015

# ViSpec – Specification Classes

Safety:

$$\square_I \phi$$

Implication:

$$\phi \rightarrow \psi$$

Reachability:

$$\diamond_I \phi$$

Reactive Response:

$$\square_I(\phi \rightarrow M_I \psi)$$

Stabilization:

$$\diamond_I \square_I \phi$$

Conjunction:

$$\phi \wedge \psi$$

Recurrence:

$$\square_I \diamond_I \phi$$

Non-strict Sequencing:

$$N_I(\phi \wedge M_I \psi)$$

$$M \in \{\square, \diamond\}, N \in \{\square, \diamond\}$$

## Motivating Example: On-Line Survey

We asked:

“At some time in the first 30 seconds, the vehicle speed ( $v$ ) will go over 100 and stay above 100 for 20 seconds”

Response:

$$\varphi = \diamond_{[0,30]}(v > 100) \Rightarrow \square_{[0,20]}(v > 100)$$

$\varphi$  is a tautology

- $(v > 100) = \perp$  any time in  $[0,30]$

$$((v > 100) \Rightarrow \square_{[0,20]}(v > 100)) = \top$$

- $(v > 100) = \top$  all the time in  $[0,30]$

$$\square_{[0,20]}(v > 100) = \top \text{ between } [0,10]$$

$$((v > 100) \Rightarrow \square_{[0,20]}(v > 100)) = \top \text{ between } [0,10]$$

- B. Hoxha and N. Mavridis and Georgios Fainekos, VISPEC: A graphical tool for easy elicitation of MTL requirements, IROS 2015



# Problem Formulation

## Problem 1 (System Independent MITL Analysis):

Given an MITL formula  $\varphi$ , find whether  $\varphi$  has any of the following logical issues:

- Validity: the specification is unsatisfiable or a tautology.
- Redundancy: the formula has redundant conjuncts.
- Vacuity: some subformulas do not contribute to the satisfiability of the formula.

## Problem 2 (System Dependent Vacuity Checking):

Given an MITL formula  $\varphi$ , and signal  $\mu$ , check whether  $\mu$  satisfies the antecedent failure mutation of  $\varphi$ .

1. A. Dokhanchi, B. Hoxha, and G. Fainekos, *Metric interval temporal logic specification elicitation and debugging*. MEMOCODE 2015, Austin, TX, USA
2. Extension of 1 under review

# Contributions

- We present a specification debugging algorithm for a fragment of Metric Interval Temporal Logic (MITL) specifications and, consequently for Signal Temporal Logic (STL).
  - We extend Linear Temporal Logic (LTL) vacuity detection algorithms to real-time specifications in MITL.
- We provide a signal vacuity detection algorithm to indicate to the testing team the signals that vacuously satisfy the specification.
- We present experimental results on specifications that typically appear in CPS specifications.

# Overview

- Motivation
- Preliminaries
- System Independent MITL Analysis
- System Dependent Vacuity Checking
- Experiments
- Conclusion & Future Research

# Metric Interval Temporal Logic: Semantic Intuition

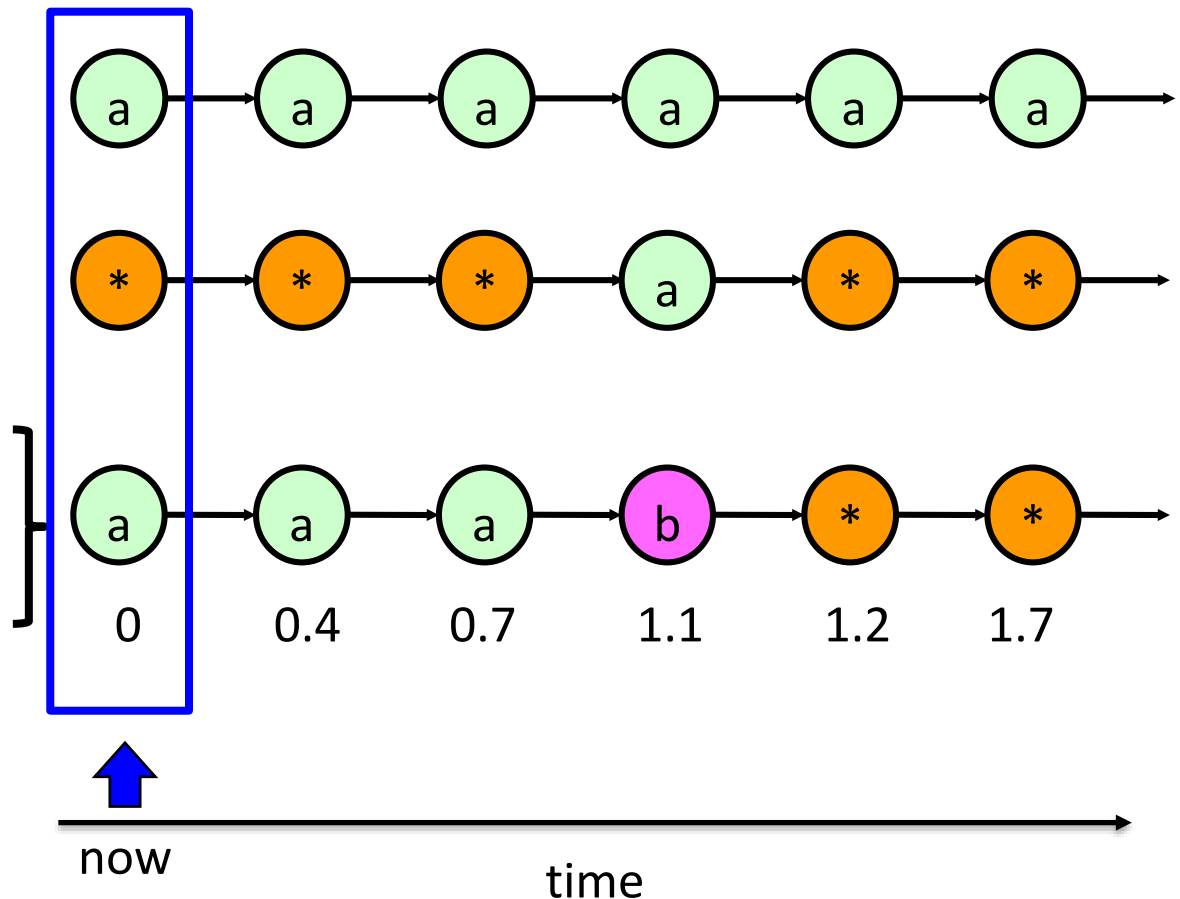
$$\phi ::= \top \mid p \mid \neg\phi \mid \phi_1 \vee \phi_2 \mid \square_I\phi \mid \diamond_I\phi \mid \phi_1 U_I\phi_2$$

$\square a$  - always a

$\diamond_{[1,3]} a$  - eventually a

$a U b$  - a until b

$a U_{[1,1.5]} b$  - a until b



# Subset of MITL

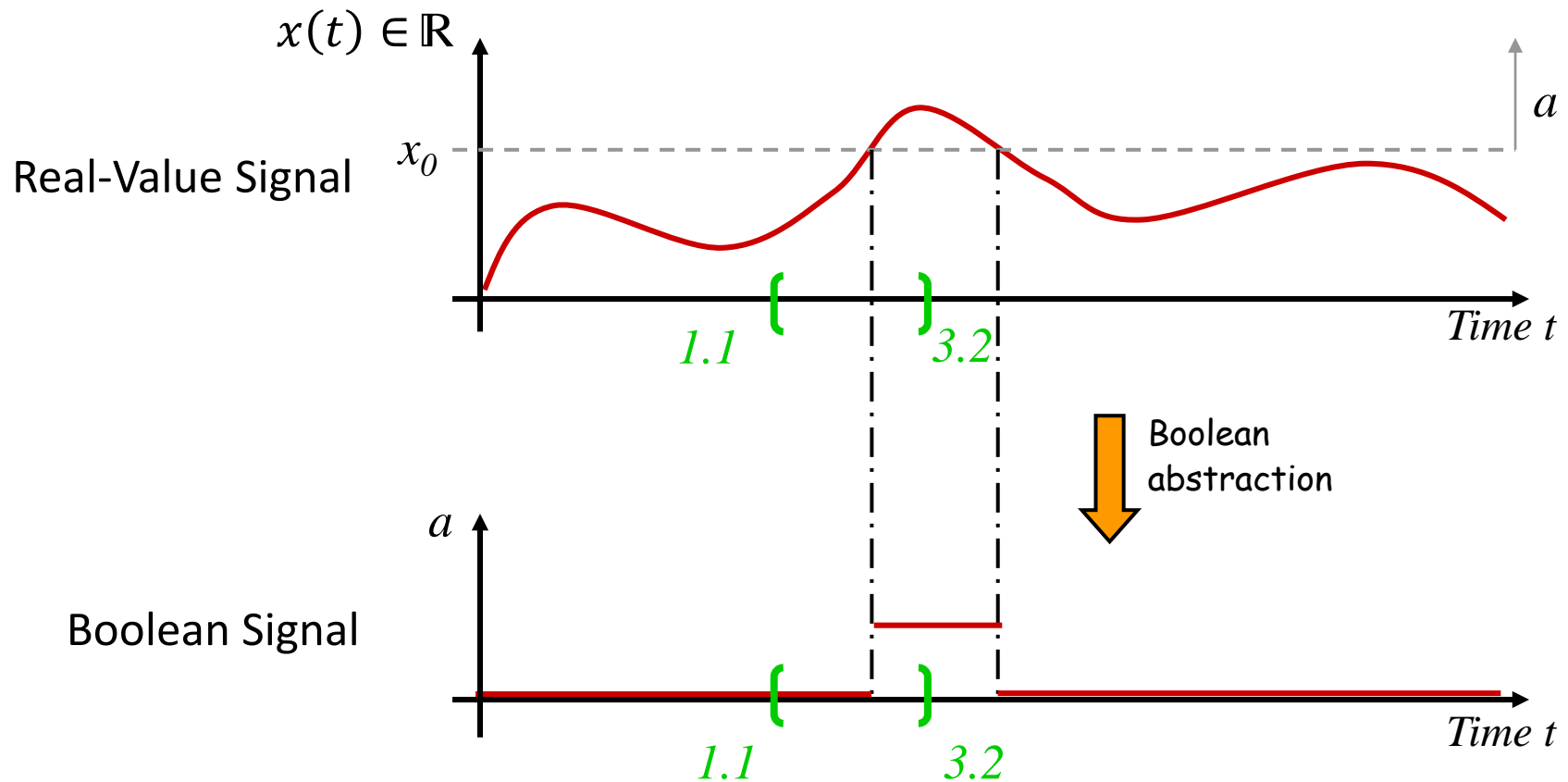
- Bounded-MITL( $\diamond$ ,  $\square$ ) with only Always & Eventually operator
- Negation Normal Form
- Syntax:

$$\phi ::= \top \mid \perp \mid p \mid \neg p \mid \phi_1 \vee \phi_2 \mid \phi_1 \wedge \phi_2 \mid \square_I \phi \mid \diamond_I \phi$$

- No Until, Release, Next operator is used

# Signal Temporal Logic

Specification example:  $\square_{[1.1,3.2]}(x(t) \geq x_0)$

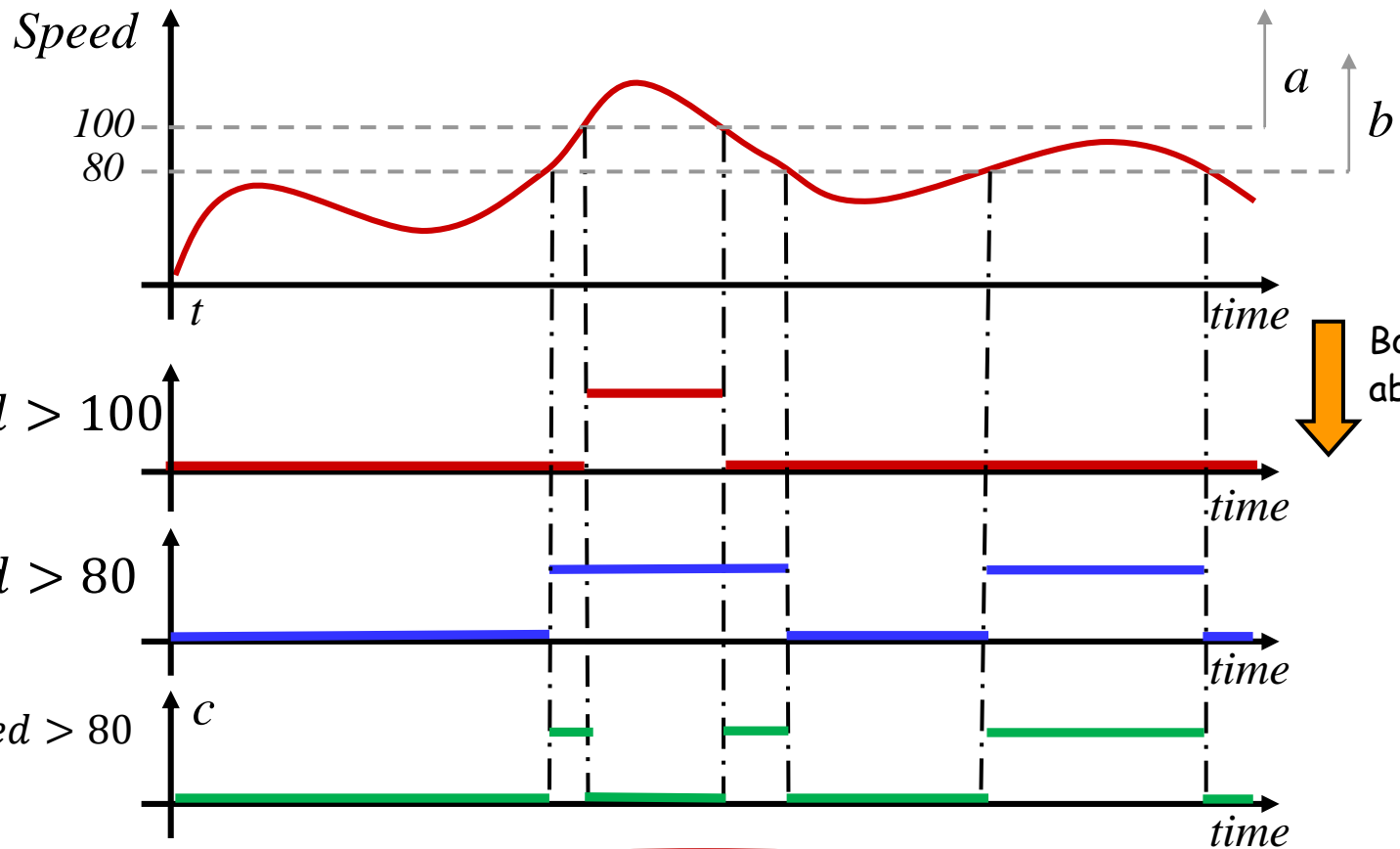


Notice example is MITL if we replace the predicate with a proposition:  $a \equiv (x(t) \geq x_0)$

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# Transforming STL to MITL



$$a \equiv \text{Speed} > 100$$

$$b \equiv \text{Speed} > 80$$

$$100 \geq \text{Speed} > 80$$

$$(speed > 100) \Rightarrow (speed > 80)$$

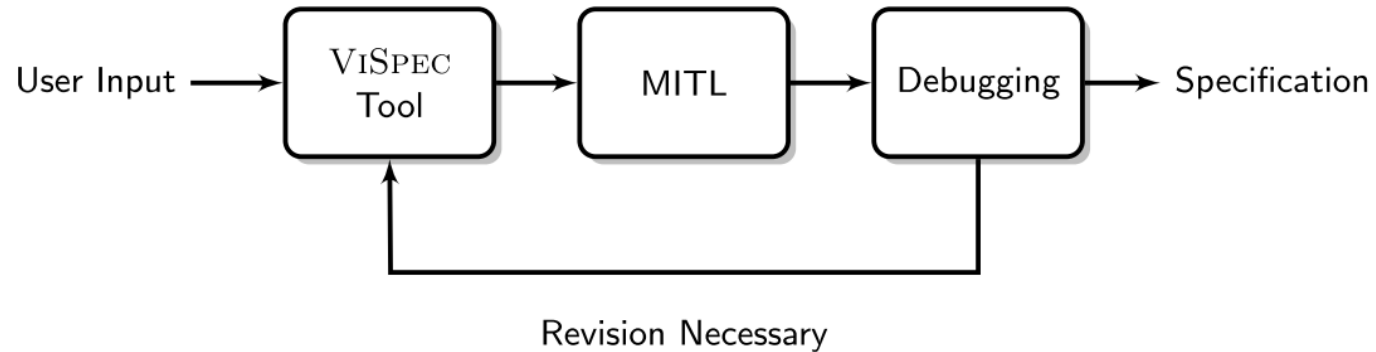
$$a \Rightarrow^? b$$

$$a \Rightarrow a \vee c$$

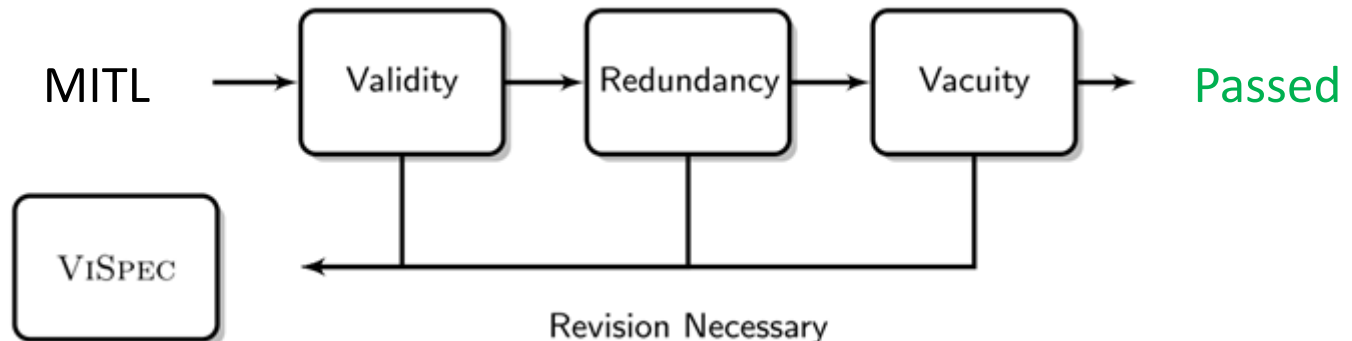


# Debugging MITL Specification

## Specification Elicitation Framework



## 3-Levels of Specification Debugging



## Validity Issues Detection

Checking whether  $\varphi$  is unsatisfiable or a tautology

A valid formula is one where  $\varphi$  and  $\neg\varphi$  are satisfiable

We asked:

“At some time in the first 30 seconds, the vehicle speed ( $v$ ) will go over 100 and stay above 100 for 20 seconds”

Response:

$$\varphi = \Diamond_{[0,30]}(v > 100) \Rightarrow \Box_{[0,20]}(v > 100)$$

$\varphi$  is a tautology

# Redundancy Issues Detection

Conjunctive formula:  $\Phi = \bigwedge_{j=1}^k \varphi_j$

Removing conjunct:

$$\bigwedge_{j=1}^{i-1} \varphi_j \wedge \bigwedge_{j=i+1}^k \varphi_j \equiv \Phi \setminus \varphi_i$$

If  $\exists \varphi_i$

$$\Phi \setminus \varphi_i \models \varphi_i$$

Then  $\varphi_i$  is redundant

**Example**  $\varphi_2 = p \wedge \square_{[0,10]} p \quad \longrightarrow \quad \square_{[0,10]} p \models p$

Algorithm 1: Checks  $\Phi \setminus \varphi_i \models \varphi_i$  for each conjunct  
Creates a list of redundant conjuncts

- H. Chockler and O. Strichman, Before and after vacuity. *Form. Methods Syst. Des.*, 34(1):37–58, Feb. 2009.

# Redundancy Example

CPS example

$$\varphi = \diamond_{[0,30]}(\text{speed} > 100) \wedge \diamond_{[0,20]}(\text{speed} > 100)$$

$\diamond_{[0,30]}(v > 100)$  is redundant since

$$\diamond_{[0,20]}(v > 100) \models \diamond_{[0,30]}(v > 100)$$

# Vacuity Issues Detection

If sub-formula  $\psi \in \varphi$  does not affect the satisfiability of  $\varphi$ , then  $\varphi$  is vacuous

Remove  $\psi$

Vacuous specifications are **equivalent** to their mutant

H. Chockler and O. Strichman, Before and after vacuity. Form. Methods Syst. Des., 34(1):37–58, Feb. 2009.

# Mutation of MITL for Vacuity Checking

Mutation with assigning  $\perp$  to literal occurrence

$$\varphi = (\neg p \wedge q) \vee \diamond_{[0,10]} p \vee \square_{[0,10]} q$$

$$\varphi[\neg p \leftarrow \perp] = (\perp \wedge q) \vee \diamond_{[0,10]} p \vee \square_{[0,10]} q$$

4 literal occurrence  $\Rightarrow$  4 mutation

Algorithm 2: Checks  $\Phi \models \varphi_i[l \leftarrow \perp]$  for each mutation  
Creates a list of mutated sub-formulas

# Vacuity Theorem

Theorem (MITL Vacuity with respect to Specification):

Assume that the specification  $\Phi$  is a conjunction of MITL formulas. If  $\exists \varphi_i \in \Phi$  and  $\exists l \in \text{litOccur}(\varphi_i)$ , such that  $\Phi \models \varphi_i [l \leftarrow \perp]$ , then  $\Phi$  satisfies  $\varphi_i$  vacuously ( $\Phi \models_v \varphi_i$ ).

We proved that in  $\Phi$

if  $\exists$  a conjunct  $\varphi_i$  & literal occurrence  $l \in \text{litOccur}(\varphi_i)$

s.t  $\Phi \models \varphi_i [l \leftarrow \perp]$

then  $\Phi$  is inherently vacuous

A. Dokhanchi, B. Hoxha, and G. Fainekos, *Metric interval temporal logic specification elicitation and debugging*. MEMOCODE 2015, Austin, TX, USA,

# Vacuity Example

CPS example

$$\varphi_{STL} = \diamond_{[0,10]}((speed > 100) \wedge \diamond_{[0,10]}(speed > 80))$$

$$\varphi = \diamond_{[0,10]}(a \wedge \diamond_{[0,10]} b) \text{ is not vacuous}$$

However...

$$\varphi' = \diamond_{[0,10]}(a \wedge \diamond_{[0,10]}(a \vee c)) \text{ is vacuous}$$

Where  $a: (speed > 100)$  and  $c: (100 \geq speed > 80)$

$$\varphi' \models \diamond_{[0,10]}(a \wedge \diamond_{[0,10]}(a \vee \perp))$$



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# Vacuous Signals

- The MITL specification

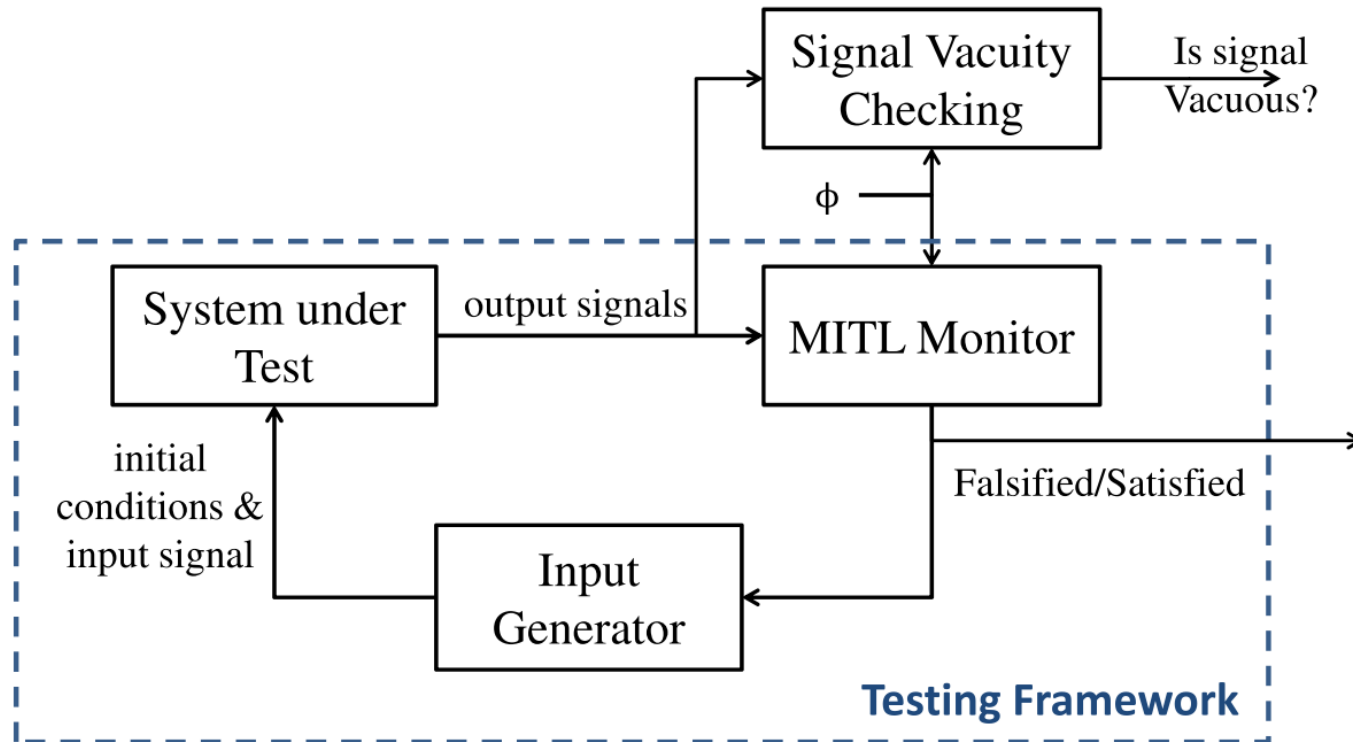
$$\varphi = \square_{[0,5]}( (request) \Rightarrow \diamond_{[0,10]}(acknowledge) )$$

- $\varphi$  is passed the MITL Specification Debugging Framework
- Any signal  $\mu$  that does not satisfy *request* at any point in time will **vacuously** satisfy  $\varphi$ .
- Signals that do not satisfy the ***antecedent (precondition)*** of the subformula are called **vacuous signals**.
- Vacuous Signals satisfy antecedent failure mutation of  $\varphi$

# Antecedent Failure Mutation

- For each implication  $(\varphi \Rightarrow \psi)$ ,  
 $(\varphi)$  is the precondition (antecedent) of the implication.
- Antecedent Failure Mutation is the assertion that the precondition  $(\varphi)$  never happens.
- Example:  
Antecedent Failure of  $\varphi$  is  $\neg\varphi$
- Signals that satisfy  $\neg\varphi$  are vacuous signals

# Vacuity Detection in Testing



# Overview

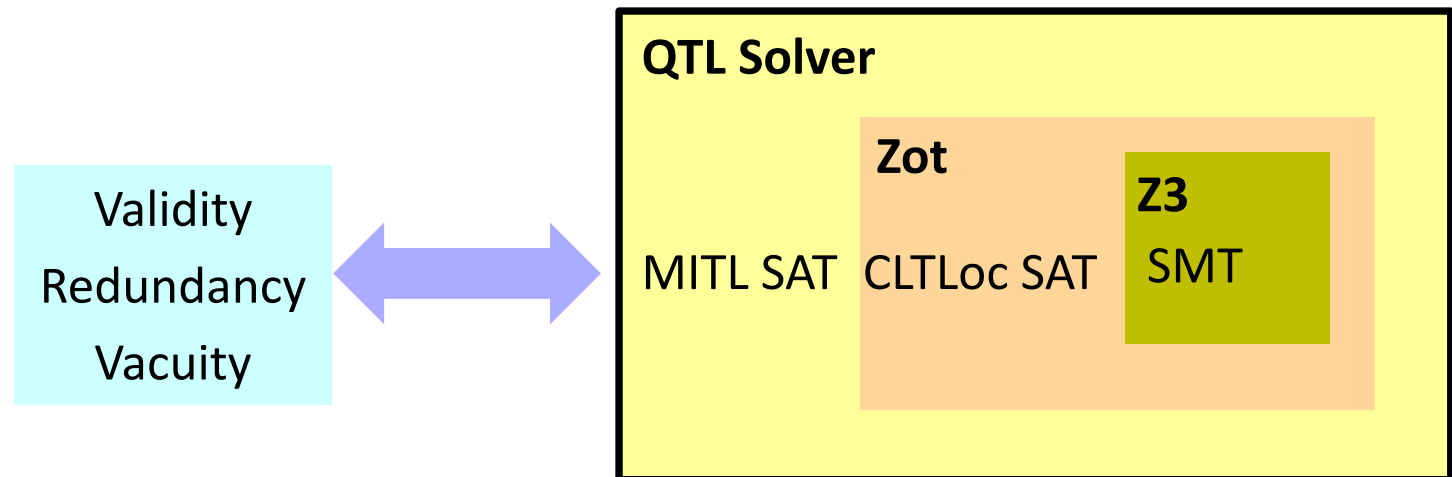
- Motivation
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# Implementation and Experiments

We used MITL satisfiability solver for this method:

$\varphi \models \psi$  iff  $(\varphi \Rightarrow \psi) \equiv T$  iff  $(\neg\varphi \vee \psi) \equiv T$  iff  $(\varphi \wedge \neg\psi) \equiv \perp$

We detected all the issues with MITL SAT solver

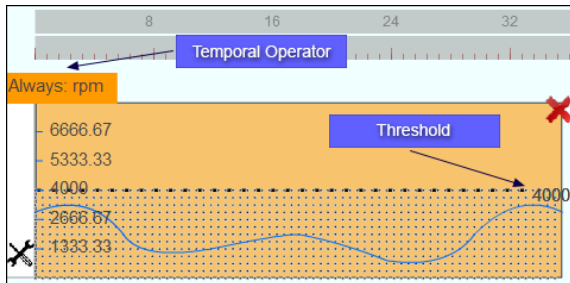


M. Bersani and M. Rossi and P. San Pietro, A tool for deciding the satisfiability of continuous-time metric temporal logic. *Acta Informatica*, pages 1–36, 2015.

# ViSpec – Usability Study

Each user received ten tasks:

- To formalize a NL specification in automotive industry through ViSpec



## Group 1: Non-expert users

No experience in working with requirements.

20 subjects from the student community at ASU

## Group 2: Expert users

Experienced in working with requirements (not necessarily formal requirements)

10 subjects from the industry in the Phoenix area

B. Hoxha and N. Mavridis and Georgios Fainekos, VISPEC: A graphical tool for easy elicitation of MTL requirements, IROS 2015

# Specification Checks

Seven of ten tasks have no detected issue

Example task with erroneous specifications:

Stabilization “*At some point in time in the first 30 seconds, vehicle speed will go over 100 and stay above for 20 seconds.*”

Correct answer:  $\diamond_{[0,30]} \square_{[0,20]}(p_1)$

$p_1$  : speed > 100

Incorrect Answers:

Specification	Detected Error
$\diamond_{[0,30]}(p_1) \wedge \diamond_{[0,20]}(p_1)$	$\diamond_{[0,30]}(p_1)$ is redundant
$\diamond_{[0,30]}(p_1 \Rightarrow \square_{[0,20]}(p_1))$	Tautology



## Error in Oscillation Task

*“At every point in time in the first 40 seconds, vehicle speed will go over 100 in the next 10 seconds.”*

Correct answer:

$$\square_{[0,40]} \diamond_{[0,10]} (p_1)$$

$p_1 : \text{speed} > 100$

Incorrect answer (with Redundancy Error):

$$\square_{[0,40]} (p_1) \wedge \square_{[0,40]} \diamond_{[0,20]} (p_1)$$

Issue:

$\square_{[0,40]} \diamond_{[0,20]} (p_1)$  is redundant

# Error in Long Sequence Task

*“If, at some point in time in the first 40 seconds, vehicle speed goes over 80 then from that point on, if within the next 20 seconds the engine speed goes over 4000, then, for the next 30 seconds, the vehicle speed should be over 100.”*

$$\diamond_{[0,40]} ( (\text{speed} > 80) \Rightarrow \diamond_{[0,20]} (\text{rpm} > 4000 \Rightarrow \square_{[0,30]} \text{speed} > 100) )$$

↓(STL2MITL)

$$\diamond_{[0,40]} ((p_1 \vee p_3) \Rightarrow \diamond_{[0,20]} (p_2 \Rightarrow \square_{[0,30]} p_1) )$$

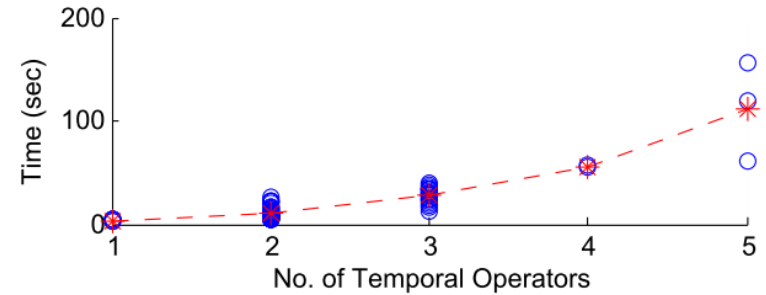
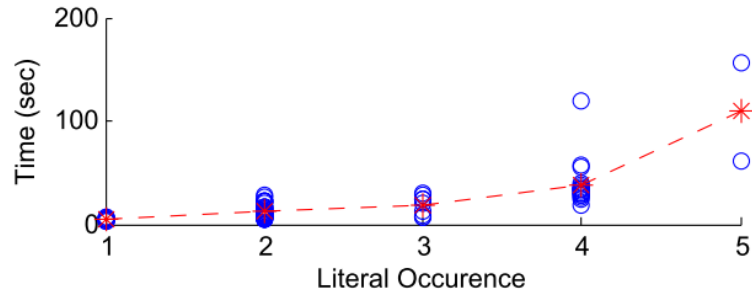
$p_1$ : speed > 100       $p_2$ : rpm > 4000       $p_3$ : 100 ≥ speed > 80

Incorrect Answers:

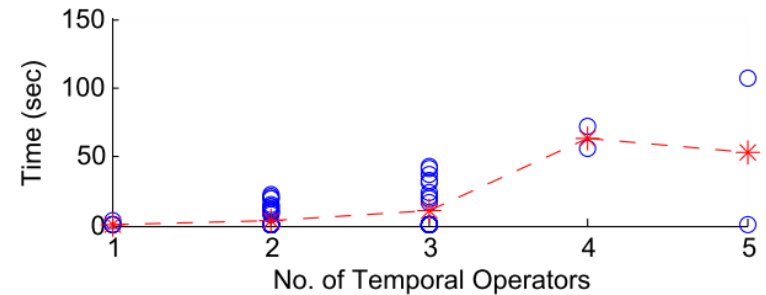
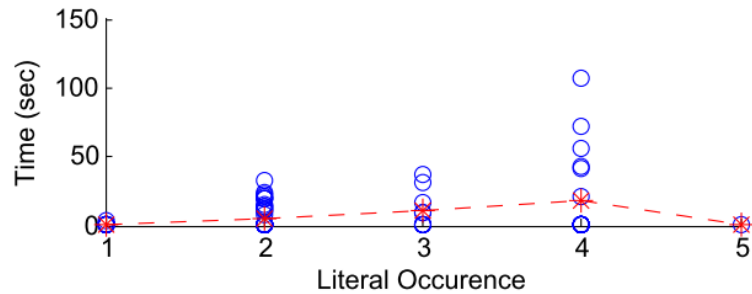
Specification	Detected Error
$\diamond_{[0,40]} ((p_1 \vee p_3) \Rightarrow \diamond_{[0,20]} p_2 \wedge \square_{[0,30]} p_1) )$	Vacuous formula
$\diamond_{[0,40]} (p_1 \vee p_3) \wedge \diamond_{[0,40]} p_2 \wedge \diamond_{[0,40]} \square_{[0,30]} p_1$	$\diamond_{[0,40]} (p_1 \vee p_3)$ is redundant

# Runtime Overhead

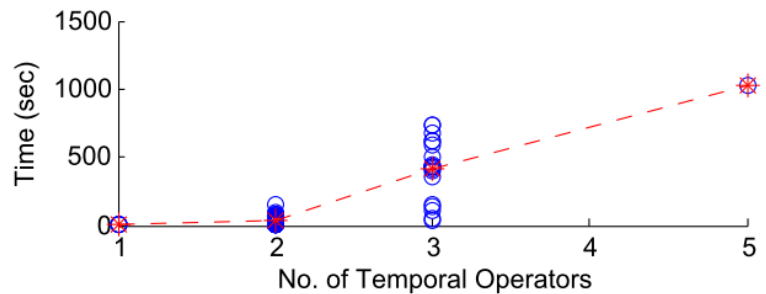
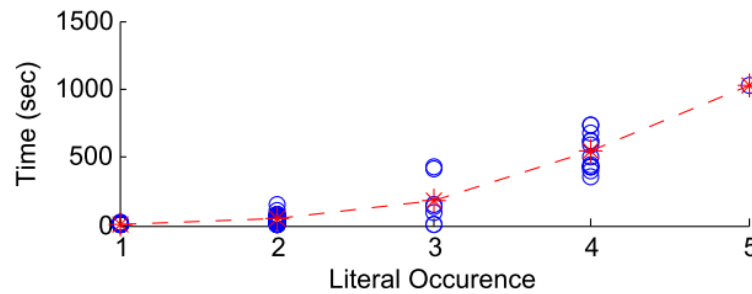
## Validity



## Redundancy



## Vacuity



# Antecedent Failure Detection

Requirement	Natural Language	MITL Formula
$\phi_1^{AT}$	There should be no transition from gear two to gear one and back to gear two in less than 2.5 sec.	$\square_{[0,27.5]}((g_2 \wedge \diamond_{(0,0.04]}g_1) \Rightarrow \square_{[0,2.5]}\neg g_2)$
$\phi_2^{AT}$	After shifting into gear one, there should be no shift from gear one to any other gear within 2.5 sec.	$\square_{[0,27.5]}((\neg g_1 \wedge \diamond_{(0,0.04]}g_1) \Rightarrow \square_{[0,2.5]}g_1)$
$\phi_3^{AT}$	If the engine speed ( $\omega$ ) is always less than 4500, then the vehicle speed ( $v$ ) can not exceed 85 in less than 10 sec.	$\square_{[0,30]}(\omega \leq 4500) \Rightarrow \square_{[0,10]}(v \leq 85)$
$\phi_3^{AT}$	Within 10 sec. the vehicle speed is less than 80 and from that point on the speed engine is always less than 4500.	$\diamond_{[0,10]}((v \leq 80) \Rightarrow \square_{[0,30]}(\omega \leq 4500))$

Requirement	Antecedent Failure	Vacuous Signals / All Signals
$\phi_1^{AT}$	$\square_{[0,27.5]}\neg(g_2 \wedge \diamond_{(0,0.04]}g_1)$	1989 / 2000
$\phi_2^{AT}$	$\square_{[0,27.5]}\neg(\neg g_1 \wedge \diamond_{(0,0.04]}g_1)$	1994 / 2000
$\phi_3^{AT}$	$\neg\square_{[0,30]}(\omega \leq 4500)$	60 / 214
$\phi_3^{AT}$	$\square_{[0,10]}\neg(v \leq 80)$	1996 / 2000

B. Hoxha, H. Abbas and Georgios Fainekos, Benchmarks for Temporal Logic Requirements for Automotive Systems, ARCH 2014

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# Conclusions

- We developed a debugging framework for MITL
- We extended the existing LTL vacuity detection algorithms to MITL
- We used utility result to check that specification is common
- We implemented the antecedent failure detection algorithm that can find signal vacuity
- Our tool can improve the users ability to create correct MITL specifications

# Future Research

- Integrate MITL analysis into ViSpec
- Finding the Coverage of specification with respect to falsifying signals
- Improving the stochastic search algorithms for falsification of the requirement in CPS with signal vacuity detection.

# Acknowledgements

**On-Line Survey:** <http://goo.gl/forms/YW0reiDtgi>

## Sponsors



NSF awards:  
IIP-1454143  
CNS-1116136  
CNS-1350420  
CNS-1319560

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